

4E4131

ROll No. LYECTEC 017

Total No of Pages: 4

4E4131

B.Tech. IV-Sem (Main & Back) Exam; June-July 2016 Electronics & Communication 4EC2A Random Variables & Stochastic Processes

Time: 3 Hours

**Maximum Marks: 80** 

Min. Passing Marks (Main & Back): 26

Min. Passing Marks (Old Back): 24

Instructions to Candidates:-

Attempt any five questions, selecting one question from each unit. All Questions carry equal marks. Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly.

Units of quantities used/calculated must be stated clearly.

Use of following supporting material is permitted during examination.

(Mentioned in form No.205)

1. NIL

2. NIL

### UNIT-I

Q.1 (a) Prove that  $2^n - (n+1)$  equations are needed to establish the mutual independence of n – events [8]

(b) The age of a person when he dies is denoted by t. The probability that  $t \le t_0$  is given by the following equation

$$P\left(t \le t_0\right) = \int_0^{t_0} A(t) dt$$

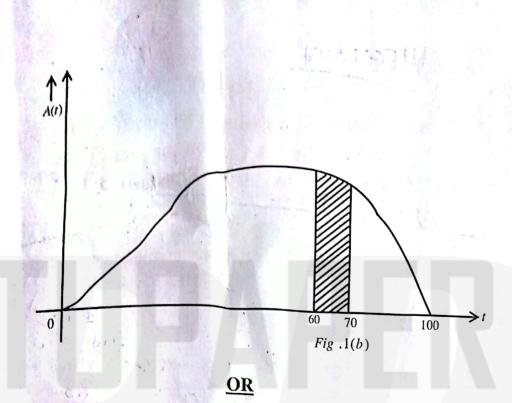
Where A(t) is a function determined from mortality records. The curve between A(t) and t is given in Fig.1(b) for  $0 \le t \le 100$  years and A(t) is given as  $A(t) = 3 \times 10^{-9} t^2 (100 - t)^2$ ;  $0 \le t \le 100$  years.

Determine the probability that a person will die between the ages of 60 & 70 assuming that he was alive at 60. [8]

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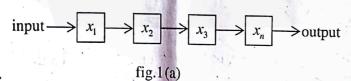
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Q.1 (a) In a system, there are n components connected in series. This system works successfully when all units (components) work successfully. The operation of each component is independent to each other. The probability of successful probability that the system functions satisfactorily.

[8]



(b) State & explain the theorem of total probability & Bayes Theorem. [8]

## UNIT-II

- Q.2 (a) Explain all the properties of conditional Distribution.
  - (b) Determine the mean and variance of the random variable X of the following distribution
    - (i) Uniform distribution
    - (ii) Exponential distribution

[5]

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[6]

[5]



# OR

Q.2	2 (a)	Determine the mean and variance of the random variable X of the follow distribution	ving
1 1		(i) Normal distribution	[5]
		(ii) Rayleigh distribution	[5]
	(b)		ible.
		Hence find the probability of 5 or more telephone calls arriving in a simil. pe	iiou
		in a collage switch board, if the telephone calls that are arrived at the rate	01 2
		every 3min. Follow a Poisson distribution.	[6]
		UNIT-III	ith
Q.3	(a)	Consider $Z = X + Y$ , show that if X and Y are independent Poisson's RV's	roı
		parameters $\lambda_1$ and $\lambda_2$ respectively, then Z is also a Poisson Random variable.	. [o] ,
	(b)	Let X and Y be the independent random variables with common parameter	.5 /0.
4		Define $U = X + Y$ , $V = X - Y$ . Find the joint and marginal pdf of U and V.	[8]
/		<u>OR</u>	
Q.3	(a)	A voltage V is a function of time t and is given by	
		$V(t) = X \cos wt + Y \sin wt$	
<b>有</b> 其前		In which w is a constant angular frequency and $X = Y = N(0, \sigma^2)$ and they	are
7.5		independent	[[0]
3		(i) Show that V(t) may be written as	
		$V(t) = R\cos(wt - \theta)$ (1) Fig. 1.4 and 1.5 and 0. are independent.	
	4.	(ii) Find the pdfs of RV's R and $\theta$ and show that R and $\theta$ are independent.	o of
1	(b)	Define a two dimensional random variable. Give an example of the out – come a random experiment, that is a two dimensional random variables.	
13	Est		[6]
	. 4	<u>UNIT-IV</u>	
Q.4	(a)	Consider a continuous random variable X, prove that	
. 0		$E[X] = \int_0^\infty [1 - F_X(x)] dx - \int_0^\infty F_X(x) dx$	
		Where $F_X(x)$ is the cdf of $X$ .	[6]
1	(b)	Explain the followings;	4
		(i) Liapounoff's form of CLT.	[5]
		(ii) Lindberg – Levy's form of CLT.	[5]
•		Where CLT = Central Limit Theorem.	
	1.		
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Q.4 (a) Consider the random variable X whose characteristics function is given by

$$\varphi_{X}(w) = \begin{cases} 1 - |w| ; |w| < 1 \\ 0 ; |w| > 1 \end{cases}$$

[8] Determine the pdf of X.

The Moment generating function of a random variable X is given by

$$M_{X}(\Omega) = \frac{5}{5 - \Omega}$$

[4] Determine the standard deviation of X. [4] -

(c) Write down all the properties of characteristics function  $\phi_x(w)$ .

## UNIT-V

[8] Write and explain all the properties of power spectral density. Q.5 (a)

Let X(t) be the WSS process with the auto correlation function given by

$$R_{XX}(\tau) = \left(\frac{A_0^2}{2}\right) \cos(w_0 \tau)$$

Where  $A_o$  and  $w_o$  are constants. Determine the psd of X(t).

[8]

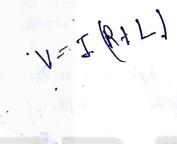
[10]

In the figure given below, X(t) be a input voltage to a circuit and Y(t) be the output voltage. The process X(t) is a stationary random process with zero mean Q.5 (a) and auto correlation

$$R_{XX}(\tau) = \bar{e}^{\alpha|\tau|}$$

Determine E[Y(t)],  $S_{YY}(w)$  and  $R_{YY}(\tau)$ .

X(t)



The psd of white noise  $\left(\frac{N_0}{2}\right)$  is  $6 \times 10^{-6}$  W/ Hz., is applied to an ideal Low Pass

Filter with power transfer function 1 and bandwidth W rad/sec. Find W so that output average noise power is 15 watt. [6]

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